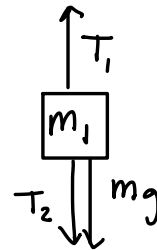
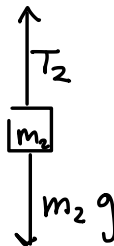
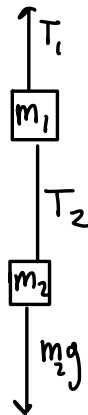
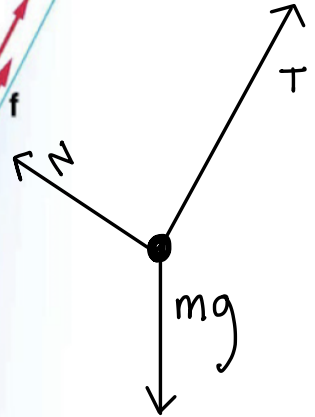
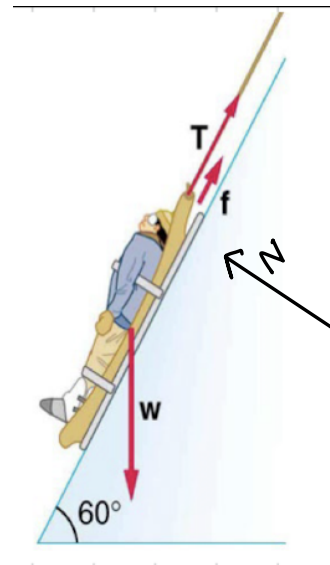
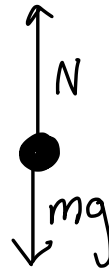
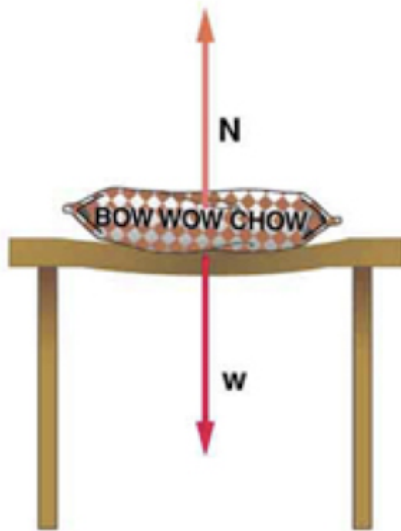


Forces

Free Body diagram

Draw the free-body diagrams for the images shown below



Practice

An arrow is shot from a height of 1.5 m toward a cliff of height H. It is shot with a velocity of 30 m/s at an angle of 60° above the horizontal. It lands on the top edge of the cliff 4.0 s later.

$$U_o = 30 \text{ m/s} \quad \theta = 60^\circ \quad h_1 = 1.5 \text{ m} \quad h_2 = ? \quad h_{\text{Tot}} = ? \quad t = 4 \text{ s}$$

$$U_{oy} = 30 \sin 60^\circ \quad U_{ox} = 30 \cos 60^\circ$$

(a) What is the height of the cliff?

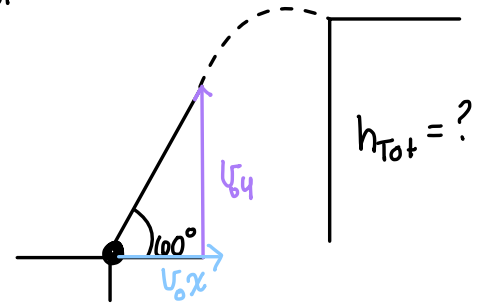
$$H_{\text{Tot}} = h_1 + h_2 = 1.5 + ?$$

$$y_2 = U_{oy} t + \frac{1}{2} g t^2$$

$$y_2 = 30 \sin 60^\circ \cdot 4 + \frac{1}{2} \cdot -9.8 \cdot 4^2$$

$$y_2 \approx 26 \text{ m}$$

$$26 \text{ m} + 1.5 \text{ m} = 27.5 \text{ m} \approx 28 \text{ m}$$



(b) What is the maximum height reached by the arrow along its trajectory?

$$H_{\text{max}} = \frac{U^2}{2g} = \frac{26^2}{2 \cdot 9.8} = 34.5 \text{ m} \approx 35 \text{ m}$$

(c) What is the arrow's impact speed just before hitting the cliff.

$$\textcircled{d} \cos \theta = \frac{a}{h}$$

$$U_{iy} = 30 \cos (60^\circ) = 15 \text{ m/s}$$

$$U_{fx} = U_{iy} = 15 \text{ m/s}$$

$$U_{fy} = U_{iy} + at$$

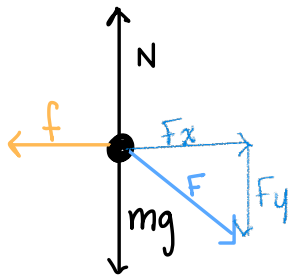
$$U_{fy} = 26 + -9.8 \cdot 4$$

$$U_{fy} = -13 \text{ m/s}$$

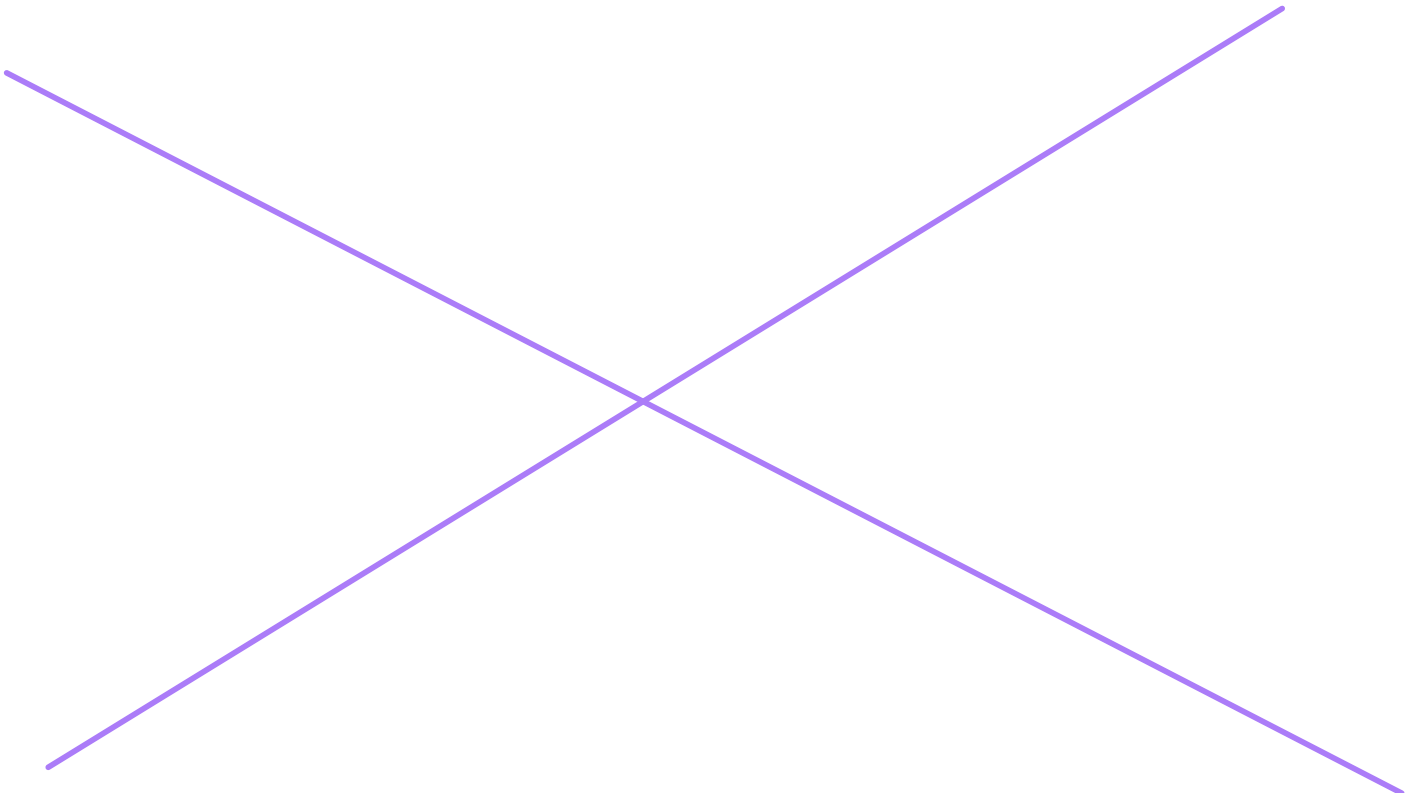
$$R = \sqrt{13^2 + 15^2} = 20 \text{ m/s}$$

A nurse pushes a cart by exerting a force on the handle at a downward angle 35.0° below the horizontal. The loaded cart has a mass of 28.0 kg , and the force of friction is 60.0 N .

(a) Draw a free-body diagram for the system of interest.



(b) What force must the nurse exert to move at a constant velocity?

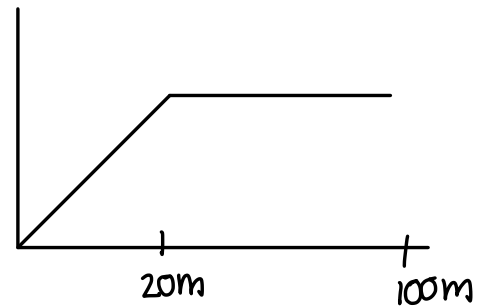


A 63.0-kg sprinter starts a race with an acceleration of 4.20 m/s^2 . What is the net external force on him? If the sprinter then accelerates at that rate for 20 m, and then maintains that velocity for the remainder of the 100-m dash, what will be his time for the race?

$$m = 63.0 \text{ kg} \quad a = 4.20 \text{ m/s}^2 \quad d_1 = 20 \text{ m} \quad d_{\text{tot}} = 100 \text{ m} \quad d_2 = d_T - d_1 = 80 \text{ m}$$

① $F = ma$

$$F = 63 \text{ kg} \cdot 4.2 \text{ m/s}^2 = 264 \text{ N}$$



Step 1:

$$t_1 = \sqrt{\frac{2d}{a}} = \sqrt{\frac{2 \cdot 20}{4.2}} = 3.086 \text{ s}$$

Step 2:

$$v = \cancel{v_0} + at = 4.2 \cdot 3.086 = 12.96 \text{ m/s}$$

Step 3:

$$t_2 = \frac{d_2}{v} = \frac{80}{12.96} = 6.17 \text{ s}$$

Step 4:

$$t_{\text{tot}} = t_1 + t_2 = 3.86 + 6.17 = 9.26 \text{ s}$$

A 63.0-kg sprinter starts a race with an acceleration of 4.20 m/s^2 . What is the net external force on him? If the sprinter then accelerates at that rate for 20 m, and then maintains that velocity for the remainder of the 100-m dash, what will be his time for the race?

$$\begin{aligned} \text{mass} &= 63.0 \text{ kg} \\ a &= 4.2 \text{ m/s}^2 \\ d_1 &= 20 \text{ m} \\ d &= 100 \end{aligned}$$

$$F = ma = 63 \cdot 4.2 = 264 \text{ N}$$

$$t = \sqrt{\frac{2d_1}{a}} = \sqrt{\frac{2 \cdot 20}{4.2}} = 3.086 \text{ s}$$

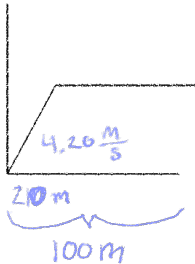
$$V = v_0 + at_1$$

$$V = at_1 = 4.2 \cdot 3.086 = 12.96$$

$$d_2 = 100 - 20 = 80$$

$$t = t_1 + t_2 = 3.086 + 6.17 = 9.265$$

$$t_2 = \frac{d_2}{V} = \frac{80}{12.96} = 6.17$$



The net external force is 264.6 N for a total time of about 9.26 s

$$a = \frac{v}{t}$$